Native defects and hydrogen impurities in Ag₃PO₄

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(Received 22 March 2012; revised manuscript received 2 June 2013; published 17 June 2013)

Silver orthophosphate (Ag₃PO₄) exhibits extremely high photocatalytic activity under visible light. Gaining insight into the behavior of point defects would open opportunities for new applications. Our hybrid density-functional calculations show that intrinsic point defects are unlikely to cause carrier trapping. Charge neutrality analysis suggests that Ag_3PO_4 possibly behaves as a weak *n*-type semiconductor under the O-poor condition and as a weak *p*-type semiconductor under the O-rich condition. Unlikely to other oxides, unintentionally incorporated hydrogen does not necessarily lead to strong *n*-type conductivity. Migration properties of some Ag-related defects and hydrogen are also discussed.

DOI: 10.1103/PhysRevB.87.245205

PACS number(s): 61.72.Bb, 61.72.S-, 71.55.Ht

Semiconductor photocatalysis has attracted much attention in recent decades due to its technological importance in clean-fuel production and environmental remediation from solar energy.¹ Photoexcited carriers occurred in photocatalysis are involved in two competing processes: (i) diffusion to the surface such that chemical reactions with adsorbed molecules can occur; and (ii) recombination, which decreases the number of active carriers consumed by chemical reactions on the surface. Therefore, it is important to promote electron-hole separation for the enhancement of photocatalytic activity. Carrier recombination is believed to be accelerated by trapping centers, which are formed by defects in a crystalline semiconductor. In a study of Nb-doped TiO₂ it was argued that deep states act as recombination centers and degrade the photocatalytic activity.² It was also shown that doping anatase TiO2 with a high concentration of nitrogen is disadvantageous for photocatalytic efficiency, probably due to defect formation.³ Recently, Kong *et al.*⁴ demonstrated that decreasing the relative concentration of bulk defects with respect to surface defects in TiO₂ leads to enhanced high photocatalytic performance. These observations underscore the significance of understanding the role of defects in photocatalysts.

The large band gap of $\sim 3.2 \text{ eV}$ in TiO₂ implies that the photocatalytic activity is triggered only under ultraviolet light and doping is a common treatment for sensitizing it under visible-light irradiation although external doping is usually accompanied by the creation of recombination centers. In contrast, some silver-based oxides such as AgNbO₃, AgAlO₂, and AgGaO₂ are photosensitive under visible light⁵⁻¹¹ and enable solar energy conversion without the need for doping. Therefore, it is important to understand their intrinsic properties such as the nature of native defects to reveal the origin of their preferred photocatalytic activities.

Recently, it has been reported that semiconductor Ag_3PO_4 exhibits extremely high photocatalytic activity with strong oxidation power leading to a high quantum yield of nearly 90% for the production of oxygen from water under visible

light.⁶ This is intriguing because most photocatalysts give much poorer quantum yields of ~20%. The outstanding photocatalytic properties of Ag₃PO₄ have triggered theoretical investigations of their origin.^{12–14} However, unanswered questions still remain such as why Ag₃PO₄ possesses superior quantum efficiency to other photocatalysts. The nature of native defects and unintentionally doped impurities in Ag₃PO₄ should have correlations with its unique properties.

Given the fact that Ag_3PO_4 is a semiconductor with a band gap of 2.4 eV and a relatively small effective mass of electron¹² (compared to that of In_2O_3), it might be applicable to optoelectronic devices. Indeed, crystalline thin film of Ag_3PO_4 has been grown and used as photoanode in a photoelectrochemical cell, suggesting that Ag_3PO_4 is an *n*-type semiconductor.⁶ Moreover, Ag_3PO_4 is a known ionic conductor in which the transportation of ions is reportedly assisted by defects.^{15,16}

Ma *et al.*¹³ used the local-density approximation with on-site Coulomb interactions (LDA + U method) to suggest theoretically that the silver vacancy (V_{Ag}) in Ag₃PO₄ is a shallow acceptor. However, there is no unique way to determine the value of U, and it is very hard to judge whether the adopted U gives reasonable results for the defect properties under the circumstances that experimental results are still limited. This is especially because the band gap of Ag₃PO₄ is largely underestimated in LDA (0.1 eV) compared to the experimental value (2.4 eV), and the position of the gap state associated with a defect, strongly depends on the U parameter.

Here we perform density-functional calculations using a screened hybrid functional, which has been proven to reliably describe the electronic and structural properties of defects in semiconductors,^{17,18} to investigate the influence of native point defects and unintentionally doped hydrogen on the photocatalytic and electrical properties of Ag_3PO_4 . Our findings are summarized as follows. (i) It is very unlikely that intrinsic point defects in Ag_3PO_4 cause the degradation of the photocatalytic activity or become the source of the electrical conductivity. (ii) Silver vacancies are abundant in as-grown



FIG. 1. (Color online) Formation energies as a function of the Fermi level (referenced to the valence-band maximum) of native point defects and interstitial hydrogen in Ag_3PO_4 , under (a) O-poor and (b) O-rich growth conditions.

Ag₃PO₄ and highly mobile, thus are expected to be the origin of ionic conductivity. (iii) Hydrogen, which is often responsible for *n*-type conductivity in other oxides, is unlikely to be a main source of electron carriers in Ag_3PO_4 .

Our calculations employed the screened hybrid functional proposed by Heyd, Scuceria, and Ernzehof (HSE),¹⁹ as implemented in the VASP code.²⁰ The use of 33% of the HF exchange potential yielded a direct band gap of 2.49 eV, in excellent agreement with the experimental value of 2.45 eV.⁶ In order to simulate point defects and impurities, we used 128-atom supercells, a shifted $1 \times 1 \times 1$ Monkhorst-Pack *k*-point set for the integration over the Brillouin zone, and a plane-wave basis set with an energy cutoff of 300 eV. The details for calculating formation energies can be found in Supplemental Material.²¹

Figure 1 shows the formation energies of V_{Ag} , oxygen vacancy (V_0) , silver interstitial (Ag_i) , oxygen interstitial (O_i) , and interstitial hydrogen (H_i) calculated under the oxygenpoor (silver-rich) and oxygen-rich (silver-poor) growth conditions. Note that the formation energies of $V_{\rm P}$, P_i , and the antisites O_{Ag} , Ag_O are found to be relatively high and thus are not shown in Fig. 1. Other antisite defects which are Ag_P, P_{Ag}, O_P, and P_O are not considered here because the ionic radii of the constituents of the antisite are very different. Those antisite defects are expected to have very high formation energies and thus are unlikely to form in a significant amount under thermodynamic equilibrium. The nature of the chemical bonding in Ag₃PO₄ suggests that the removal of an Ag atom to form V_{Ag} should not cost much energy because it involves the breaking of weak Ag-O bonds. This is reflected by the low formation energy of V_{Ag} even under the silver-rich condition. The absence of an Ag atom creates partially occupied states in the band gap [Fig. 3(a)], mostly derived from the d orbitals of a neighboring Ag atom. These states can accept an additional electron, thus making the V_{Ag} a single acceptor. The transition level at which the stable charge state changes from neutral to singly negative $\varepsilon(0/-)$ is located at 0.62 eV above the valence band maximum (VBM) for V_{Ag} , indicating that V_{Ag} is a deep acceptor. The method used for calculating defect transition levels is described in Ref. 22. Since V_{Ag} is an acceptor, V_{Ag}



FIG. 2. (Color online) Atomic structures in the vicinity of (a) V_{Ag}^{-} , (b) Ag_i^{+} , (c) V_0^{2+} , (d) O_i^0 (split), and (e) H_i^{+} . The directions in which neighboring atoms relax are selectively shown by arrows. The ideal positions of atoms removed to form vacancies are indicated by empty circles.

in the negative charge state (V_{Ag}^{-}) is more easily formed when ε_F increases and thus becomes predominant in Ag₃PO₄ for $\varepsilon_F > 0.62$ eV, which is indicated by the very low formation energy under both of the growth conditions shown in Fig. 1. Inward relaxations were observed at the two nearest-neighbor Ag atoms upon the formation of a V_{Ag} in both charge states. The distance of the two Ag atoms across the V_{Ag} is ~16% shorter than the equilibrium distance of the corresponding two Ag atoms in the perfect crystal [see Fig. 2(a)]. This indicates the presence of strong attractive interactions between the V_{Ag} and the neighboring Ag atoms, possibly leading to high V_{Ag} mobility. We investigated this aspect by computing the migration barrier of V_{Ag}^{-} . The calculated migration barrier is very low (0.10 eV), thus a V_{Ag}^{-} is likely to migrate along the path involves the displacement of a nearest-neighbor Ag atom along the [001] direction (see Fig. 2). A barrier of this magnitude can readily be overcome even at room temperature, indicating that although a high concentration of silver vacancies can be formed during growth, they are unlikely to remain as isolated vacancies; they will bind with other defects or impurities, diffuse out of the bulk region, or possibly migrate and become trapped at surface of the Ag₃PO₄ particle. Combined with the fact that it possesses a deep $\varepsilon(0/-)$ transition level, V_{Ag} is unlikely to render Ag₃PO₄ a *p*-type semiconductor.²³

Silver interstitial [Fig. 2(b)] favors the tetrahedral site coordinated by four O atoms. Here Ag_i acts as a shallow donors, being stable only in 1 + charge state such that $\varepsilon(+/0)$ is located above the conduction-band minimum (CBM). The formation energy of Ag_i in Ag_3PO_4 is relatively low compared to the corresponding defects in other oxides such as Zn_i in ZnO^{23} and Sn_i^{24} in SnO_2 under cation rich condition [Fig. 1(a)]. However, our calculations show that Ag_i can readily migrate along the [100] interstitial channel with a low migration barrier of 0.25 eV.²⁵ This implies that although Ag_i might be formed during growth, they are highly mobile even at room temperature. Therefore, it is very unlikely that Ag_i cause the *n*-type conductivity of Ag_3PO_4 .

Oxygen vacancy in Ag₃PO₄ has a relatively high formation energy (Fig. 1) compared to V_{Ag} and Ag_i because the strong P-O bond must be broken to remove an O atom. The transition level $\varepsilon(2 + 10)$ is located at 1.12 eV below the CBM indicating that V_0 is a very deep donor. The V_0 presents in the 2 + charge state when ε_F is near the VBM, at which the V_O-related states, are empty and located close to the CBM. When ε_F is located near the CBM, the V_0 is energetically stable in charge neutral, and gives rise to fully occupied states near the VBM. The 1+ charge state is unstable for the entire range of ε_F considered here, indicating "negative-U" behavior in which $\varepsilon(2 + /+)$ lies above $\varepsilon(+/0)$. This behavior arises from large differences in the local atomic relaxations for $V_{\rm O}$ in different charge states. It is interesting to note that the $V_{\rm O}$ -related states in Ag₃PO₄ possess the characteristic of the valence band, mainly derived from O and P p orbitals, and Ag d orbitals,²¹ in contrast to other metal oxides such as ZnO, SnO_2 where the V_0 -related states are mainly derived from metal s orbital, having the characteristic of the conduction band.

Another relatively low energy defect is interstitial oxygen. We find that extra oxygen atoms are energetically favorable in the split-interstitial configuration, O_i (split).²³ Here the calculated O-O bond length is 1.45 Å, compared to 1.20 Å for the isolated O_2 molecule, indicating that the $pp\pi^*$ -like molecular orbital of the O_i (split) is filled by two electrons from neighboring P and Ag atoms. The O_i (split) is electrically inactive (neutral) for the most values of ε_F considered, and gives rise to an occupied state just above the VBM [Fig. 3(a)]. When the Fermi level is located very close to the VBM, O_i (split) can occur in the 2 + charge state (Fig. 1) although such conditions are unlikely in Ag₃PO₄ as discussed below.

As discussed above, native point defects are unlikely to be responsible for an intrinsic conductivity of Ag_3PO_4 , while an *n*-type character was observed in the previous report.⁶ Therefore, it is worth investigating the influence of an unintentionally doped impurity, hydrogen, which is ubiquitous and regarded as a potential donor in oxides.²⁶ In addition, precursors for synthesizing Ag_3PO_4 usually contain hydrogen, and they are possibly left in a bulk. Neither experimental nor theoretical studies for hydrogen-related impurities in Ag_3PO_4 have been reported elsewhere.

We investigated interstitial hydrogen in three charge states: positive, neutral, and negative. Similar to other oxides,^{24,26,27} H_i^+ favors sites close to oxygen [Fig. 2(e)] where a strong O-H bond of length 0.96 Å is formed, the same as the calculated



FIG. 3. (Color online) (a) Single-particle energy levels introduced in the band gap by native point defects. The arrows indicate the electron occupation. (b) Thermodynamic transition levels for native point defects and interstitial hydrogen in Ag_3PO_4 . The shaded landscape-oriented belts indicate the possible range of Fermi level associated with the two extreme growth conditions (O-rich and O-poor) of Ag_3PO_4 .

bond length in H₂O (0.96 Å). In the negative charge state, H_i^- prefers sites, closer to the cations (Ag⁺ in our case).²⁷ However, the high formation energy of H_i^- results in the $\varepsilon(+/-)$ transition level being located well above the CBM, implying that H_i^+ is stable for the entire range of ε_F values in the band gap (H_i^0 is never stable). Therefore, H_i should act as a shallow donor in Ag₃PO₄. In addition, H_i^+ has low formation energy as shown in Fig. 1. In order to reveal whether H_i remains active as donor at the temperature of interest, we investigate the migration of H_i for the two diffusion paths.²¹ The diffusion along the path involved forming new O-H bond with the next-nearest neighbor O atom yield migration barrier of ~ 0.32 eV, which is lower than those in ZnO²⁸ and SnO_2 ²⁴ This implies that H_i is highly mobile even below room temperature and therefore can diffuse out of the sample or bind with other defects. This does not reflect that O-H bond in Ag₃PO₄ is weaker than those in ZnO and SnO₂ as evident from the calculated O-H bond length of 0.96 Å. In addition, our Bader analysis²⁹ shows that an O atom in bulk Ag₃PO₄ possesses -1.49 electron, more than those in ZnO $(-1.13e)^{30}$ and SnO₂ $(-1.26e)^{31}$ This implies that O-H bonds in Ag₃PO₄ are more ionic than those in ZnO and SnO₂. In fact, the migration barrier of H_i is influenced by many factors such as the local atomic environment around the diffusion path. The complete picture of H diffusion in Ag₃PO₄ could be complex and is beyond the scope of this study.

We also found that hydrogen acts as a shallow donor when substituted for oxygen (H_O). At these sites a strong P-H bond is formed with a length of 1.40 Å, whereas no bond is formed with the three Ag atoms (the Ag-H distance is 2.84 Å). This is in contrast to the case of H_O in binary oxides such as ZnO and SnO₂, where multicenter bonds are formed leading to an *n*-type conductivity.^{24,32} In Ag₃PO₄, however, H_O⁺ can easily be dissociated to V_0^0 and H_i^+ due to their low binding energy of 0.34 eV. Combined with the fact that the formation energy of H_0^+ is higher than that of H_i^+ by 1.50 eV even under the O-poor growth condition, we can exclude the possibility that H_0 is predominant in Ag₃PO₄ under thermodynamic equilibrium.

In order to determine the Fermi level of Ag₃PO₄, we have self-consistently satisfied the condition of charge neutrality $\sum_{i} q_i c(X_i^{q_i}) - n + p = 0$, where the first term is a sum over concentration of all point defects considered in charge state q_i . n is the concentration of electrons in the conduction band and p is concentration of holes in the valence band. The detailed procedure for determining the Fermi level from the charge neutrality condition is described in Ref. 21. The defects with the lowest formation energies (highest concentration) essentially dominate in the charge neutrality. Let us consider the two extreme cases in which the realistic situation may fall somewhere in between. For the first case, all highly mobile defects which are H_i^+ , Ag_i^+ , and V_{Ag}^- are considered to be annealed out or be passivated by counter charge defects and thus become electrically inactive.²³ In this case, the concentration of the charge neutrality is satisfied among electron and hole carriers in the same way as an intrinsic semiconductor leading to the Fermi level pinned at 1.25 eV above the VBM for both O-poor and O-rich conditions. For the second case, all defects shown in Fig. 1 are taken into account for the calculation of Fermi level, which is estimated to be about the intersections of two lines for H_i^+ and V_{Ag}^- , which are about 1.62 and 0.83 eV above the VBM for the O-poor and O-rich conditions, respectively. We thus expect the realistic pinned Fermi level, is in between the two extreme cases, which is reasonably far away from the band edges. At this Fermi level, n and p are negligible and thus Ag_3PO_4 is intrinsically insulating. The analysis above also suggests that Ag₃PO₄ possibly behaves as a weak *n*-type semiconductor under the O-poor condition and as a weak *p*-type semiconductor under the O-rich condition. This behavior of an intrinsic Ag₃PO₄ is in contrast to the typical photocatalyst TiO₂ which usually shows *n*-type conductivity under an oxygen poor condition.

The calculated single-particle energy levels and thermodynamic transition levels associated with native point defects and hydrogen impurities are summarized in Fig. 3. Based on these levels, we now provide insight into the photocatalytic and electrical properties of Ag₃PO₄. The remarkably high quantum efficiency of nearly 90% implies that most of the photoexcited carriers participate in the photocatalytic reactions and that electron-hole recombination is suppressed. One origin of this property might be the large difference in the effective masses of electrons (m_{e}^{*}) and holes (m_{h}^{*}) .¹² Moreover, silver-based oxides possess the characteristic that the top of the VB is composed both of Ag d and O p orbitals.¹² This promotes carrier hopping between cation and anion sites and is thus advantageous for hole transfer.³³ However, these features alone cannot explain the unique properties of Ag₃PO₄. Recombination due to traps induced by defects or impurities is known as Shockley-Read-Hall (SRH) recombination and is promoted more by midgap defect levels than the near-edge levels.³⁴ Our results suggest that native point defects are unlikely to cause carrier recombination in Ag₃PO₄. Under the O-poor condition, where the Fermi level is pinned at $\sim 1.25 - 1.62$ eV above the VBM, the thermodynamically stable charge states of relevant defects are V_{Ag}^{-} , V_{O}^{0} , and O_{i}^{0} (split) [Fig. 3(b)] of which occupied single-particle levels (hereby referred as "defect levels") lie close to the VB edge [Fig 3(a)]. Under the O-rich condition, where the Fermi level is pinned at ~0.83–1.25 eV above the VBM, the defect levels in their thermodynamically stable charge states V_{Ag}^{-} , V_{O}^{2+} , and O_{i}^{0} (split) still lie close to the band edges. This indicates that there is no plausible carrier recombination centers associated with native defects under a realistic Fermi level of as-grown Ag₃PO₄, which partly explain the high photocatalytic activity of Ag₃PO₄ observed in Refs. 6 and 35. We note that the defect levels associated with Ag_i⁺ and H_i⁺ lie above the CBM and are thus unlikely to cause the carrier recombination. The absence of the deep states in Ag₃PO₄ is one of the reasons for its superior quantum efficiency to other photocatalysts.

Our results also suggest that native defects cannot be responsible for the electrical conductivity of Ag₃PO₄. From the thermodynamic transition levels shown in Fig. 3(b), it is apparent that V_{Ag} is a deep acceptor, and its capability of generating hole carriers is limited. In addition, the low migration barrier of V_{Ag} implies that it will not remain as isolated defect, and thus cannot act as compensating center for *n*-type doping. These properties of V_{Ag} are very contrast to that of cation vacancies in other oxides, in which the formation energy of cation vacancies and their migration barriers are relatively high. The presence of V_{Ag} in the bulk at very low temperatures might be detected by positron annihilation spectroscopy (PAS), which was successfully performed to detect V_{Zn} in ZnO.³⁶ Given that V_{Ag} is highly abundant, can be negatively charged, and has high mobility, we suggest that V_{Ag} could be responsible for the ionic conductivity observed in Ag₃PO₄.¹⁶ We also find that native defects are unlikely to cause n-type conductivity. Although Ag_i shows the characteristic of a shallow donor, it is highly mobile. $V_{\rm O}$ and O_i (split) are very deep donors and have very high formation energies [Fig. 3(b)]. Surprisingly, unlike other oxides, the unintentionally incorporated hydrogen cannot cause *n*-type conductivity, either. This is because H_i^+ is highly mobile and does not successfully generate electron carriers, while H_{Ω}^{+} , which is known as a source of *n*-type conductivity in many oxides, has a high formation energy and can easily be dissociated into V_0^0 and H_i^+ , indicating that H_0^+ is unlikely to be the primary donor. Hence, the origin of the *n*-type characteristic observed in a Ag₃PO₄ thin film in Ref. 6 was not identified in the present study. However, as we discussed above, under the O-poor condition Ag₃PO₄ can behave as a weak *n*-type semiconductor.

Since there is no potential compensating center for donors and the position of the CBM is relatively low (which implies that the donor ionization level can be very close or even above the CBM), we expect that external doping for *n*type Ag₃PO₄ is feasible with high carrier concentration. Such an *n*-type Ag₃PO₄ is required for an electrode in the photoelectrochemical cell and other applications. Our results suggest that shifting the Fermi level towards the conduction band, or in other words *n*-type conditions, likely enhance the photocatalytic activities in Ag₃PO₄. Sulfur is a possible candidate for *n*-type doping when substituted for P, as in the case of S-doped GaP which exhibits *n*-type conductivity.³⁷ Last but not least, our results also reveal that the behaviors of point defects in Ag_3PO_4 are different²¹ from those in metal oxides such as ZnO, and lead to a deep understanding of the electronic and photocatalytic properties of Ag-based oxides.

In summary, we have investigated the influence of native point defects and hydrogen impurities in Ag_3PO_4 using hybrid-functional calculations. We find that native point defects are unlikely to degrade the photocatalytic activity or be responsible for the electrical conductivity. The charge neutrality analysis suggests that Ag_3PO_4 possibly behaves a weak *n*-type semiconductor under the O-poor condition and as a weak *p*-type semiconductor under the O-rich condition. The unintentional incorporation of hydrogen does not necessarily

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cause *n*-type conductivity in contrast to other oxides. Our results suggest that Ag_3PO_4 could feasibly be doped in *n*-type fashion.

We would like to thank S. Ouyang and J. Ye for fruitful discussions and advice. N.U. thanks H. Hosono for useful advice. This work was supported by the Japan Science and Technology Agency (JST) Precursory Research for Embryonic Science and Technology (PRESTO) program. P.R. thanks J. T.-Thienprasert for useful discussion. P.R. and N.U. thank the High-Performance Computing Center of California NanoSystems Institute (CNSI, UCSB) and the Synchrotron Light Research Institute (SLRI, Thailand) for their hospitality.

- ²¹See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.87.245205 for more information on the details for partial charge density plot of oxygen vacancy, the calculations of formation energies, the growth conditions considered, and the Fermi level.
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- ²⁵This value was obtained by the nudge elastic band method (NEB). The position of the Ag_i in each NEB image was fixed while the other atoms were fully relaxed. This is to ensure the migration of the Ag_i along the [100] channel. We found that when all atoms were allowed to relax the Ag_i spontaneously moved off the [100] channel, leading to the large relaxations of the neighboring atoms. Although this finding indicates that the migration of Ag_i could be more complicated, we believe that the migration barrier of Ag_i should be relatively low and our conclusion remains.
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